

Learning Semantic Representations with Hidden Markov Topics Models

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Abstract

In this paper, we describe a model that learns semantic representations from the distributional statistics of language. This model, however, goes beyond the common *bag-of-words* paradigm, and infers semantic representations by taking into account the inherent sequential nature of linguistic data. The model we describe, and which we refer to as a *Hidden Markov Topics model* is a natural extension of the current state of the art in Bayesian bag-of-words models, i.e. the Topics model of Griffiths, Steyvers, and Tenenbaum (2007), preserving its strengths while extending its scope to incorporate more fine-grained linguistic information.

Introduction

How word meanings are learned is a foundational problem in the study of human language use. Within cognitive science, a promising recent approach to this problem has been the study of how the meanings of words can be learned from their statistical distribution across the language. This approach is motivated by the so-called *distributional hypothesis*, originally due to Harris (1954) and Firth (1957), which proposes that the meaning of a word is given by the linguistic contexts in which it occurs. Numerous large-scale computational implementations of this approach — including, for example, the work of Schütze (1992), the HAL model (Lund, Burgess, & Atchley, 1995), the LSA model (Landauer & Dumais, 1997) and, most recently, the Topics model (Griffiths et al., 2007) — have successfully demonstrated that the meanings of words can, at least in part, be derived from their statistical distribution in language.

Important as these computational models have been, one of their widely shared practices has been to treat the linguistic contexts in which a word occurs as unordered sets of words. In other words, the linguistic context of any given word is defined by which words co-occur with it and with what frequency, but it disregards all fine-grained sequential and syntactic information. By disregarding these types of data, these so-called *bag-of-words* models drastically restrict the information from which word meanings can be learned. All languages have strong syntactic-semantic correlations. The sequential order in which words occur, the argument structure and general syntactic relationships within sentences, all provide vital information about the possible meaning of words. This

information is unavailable in bag-of-words models and consequently the extent to which they can extract semantic information from text, or adequately model human semantic learning, is limited.

In this paper, we describe a distributional model that goes beyond the bag-of-words paradigm. This model is a natural extension to the current state of the art in probabilistic bag-of-words models, namely the Topics model described in Griffiths et al. (2007) and elsewhere. The model we propose is a seamless continuation of the Topics model, preserving its strengths — its thoroughly unsupervised learning, its hierarchical Bayesian nature — while extending its scope to incorporate more fine-grained sequential and syntactic data.

The Topics Model

The standard Topics model as described in Griffiths and Steyvers (2002, 2003); Griffiths et al. (2007) is a probabilistic generative model for texts, and is based on the Latent Dirichlet Allocation (LDA) model of Blei, Ng, and Jordan (2003). It stipulates that each word in a corpus of texts is drawn from one of K latent distributions $\phi_1 \dots \phi_k \dots \phi_K \doteq \phi$, with each ϕ_k being a probability distribution over the V word-types in a fixed vocabulary. These distributions are the so-called *topics* that give the model its name. Some examples, learned by a Topics model described in Andrews, Vigliocco, and Vinson (In Press), are given in the table below (each column gives the 7 most probable word types in each topic).

theatre	music	league	prison	air
stage	band	cup	years	aircraft
arts	rock	season	sentence	flying
play	song	team	jail	flight
dance	record	game	home	plane
opera	pop	match	prisoner	airport
cast	dance	division	serving	pilot

As is evident from this table, each topic is a cluster of related terms that corresponds to a coherent semantic theme, or subject-matter. As such, the topic distributions correspond to the semantic knowledge learned by the model, and the semantic representation of each word in the vocabulary is given by a distribution over them.

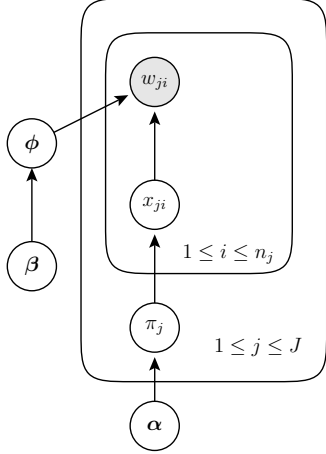


Figure 1: A Bayesian network diagram of the standard Topics model described in Griffiths et al. (2007) and elsewhere. Details are provided in the main text. Note that β denotes the parameters of a V -dimensional Dirichlet distribution, from which each of K topic distributions are sampled.

To describe the Topics model more precisely, let us assume we have a corpus of J texts $\mathbf{w}_1 \dots \mathbf{w}_j \dots \mathbf{w}_J$, where the j th text \mathbf{w}_j is a sequence of n_j words, i.e. $w_{j1} \dots w_{ji} \dots w_{jn_j}$. Each word, in each text, is assumed to be sampled from one of the model's K topics. Which one of these topics is chosen is determined by the value of a latent variable x_{ji} that corresponds to each word w_{ji} . This variable takes on one of K discrete values, and is determined by sampling from a probability distribution π_j , which is specific to text j . As such, we can see that each text \mathbf{w}_j is assumed to be a set of n_j independent samples from a mixture model. This mixture model is specific to text j , as the mixing distribution is determined by π_j . However, across texts, all mixing distributions are drawn from a common Dirichlet distribution, with parameters α . Given known values for ϕ and α , the likelihood of the entire corpus is given by

$$P(\mathbf{w}_{1:J} | \phi, \alpha) = \prod_{j=1}^J \int d\pi_j P(\pi_j | \alpha) \left[\prod_{i=1}^{n_j} \sum_{\{x_{ji}\}} P(w_{ji} | x_{ji}, \phi) P(x_{ji} | \pi_j) \right], \quad (1)$$

In this, we see that the Dirichlet distribution $P(\pi_j | \alpha)$ introduces a hierarchical coupling of all the mixing distributions. As such, the standard Topics model is a hierarchical coupling of mixture models, effectively defining a continuum of mixture models, all sharing the same K component topics.

The standard Topics model is thus an example of a *hierarchical language model*. It assumes that each text is

generated according to an elementary language model — specifically a mixture of unigram distributions — which are then hierarchically coupled with one another. From this, it is evident that the standard model can be extended by simply changing the elementary language model on which it is based. There are multiple possible language models that could be used in this respect. One possibility is to use a bigram language model as described in Wallach (2006). Another possibility is to use a language model based on a full phrase-structure grammar as described in Boyd-Graber and Blei (2009). However, in that work, the syntactic structure underlying the sentences in the texts is assumed to be known in advance, and is provided by syntactically tagged corpus. In what follows, we describe a Topics models whose elementary language model is a Hidden Markov model (HMM). We refer to this as the *Hidden Markov Topics model* (HMTM)¹.

Hidden Markov Topics model

In the HMTM, just as in the standard Topics model, each w_{ji} is drawn from one of K topics, the identity of which is determined by the latent variable x_{ji} . However, rather than sampling each x_{ji} independently from a probability distribution π_j , as in the standard model, these latent variables are generated by a Markov chain that is specific to text j . By direct analogy with the standard model, across the texts, the parameters of these Markov chains are drawn from a common set of Dirichlet distributions. As such, the HMTM is a hierarchical coupling of HMMs, defining a continuum of Hidden Markov models, all sharing the same state to output mapping.

In the HMTM, the likelihood of the corpus is

$$P(\mathbf{w}_{1:J} | \phi, \alpha, \gamma) = \prod_{j=1}^J \int d\pi_j d\theta_j P(\pi_j, \theta_j | \alpha, \gamma) \left[\sum_{\{\mathbf{x}_j\}} \prod_{i=1}^{n_j} P(w_{ji} | x_{ji}, \phi) \prod_{i=2}^{n_j} P(x_{ji} | x_{ji-1}, \theta_j) P(x_{j1} | \pi_j) \right]. \quad (2)$$

Here, θ_j and π_j are the parameters of the Markov chain of latent-states in text j . The θ_j is the $K \times K$ state transition matrix (i.e. the k th row of θ_j gives the probability of transitioning to each of the K states, given that the current state is k), and π_j is the initial distribution for the K states. The distribution over the π_j and

¹The HMTM bears some resemblance to a model described in Griffiths et al. (2007) that couples a Hidden Markov model with a standard Topics model. There are, however, substantial differences between these models. In particular, the HMTM is designed to learn semantic representations by directly availing of the sequential information in text. By contrast, the HMM based model described in Griffiths et al. (2007) learns semantic representations using a standard topics model, while the HMM is used to learn syntactic categories.

θ_j , i.e. $P(\pi_j, \theta_j | \alpha, \gamma)$, is a set of independent Dirichlet distributions, where α are the parameters for the Dirichlet distribution over π_j , and $\gamma_1 \dots \gamma_K \doteq \gamma$ are the parameters for the distribution over each of the K rows of θ_j .

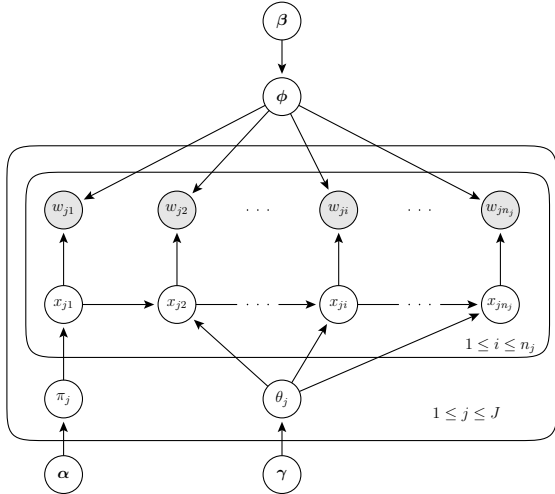


Figure 2: A Bayesian network diagram for the Hidden Markov Topic model. Details are provided in the main text.

Learning and Inference

From this description of the HMTM, as well as from its Bayesian network diagram given in Figure 2, we can see that the HMTM has four sets of parameters whose values must be inferred from a training corpus of texts. These are the K topic distributions, i.e. ϕ , the Dirichlet parameters for the latent-variable Markov chains, i.e. α and γ , and the Dirichlet parameters from which the topic distributions are drawn, i.e. β . The posterior over ϕ , α , β and γ given a set of J texts $\mathbf{w}_{1:J}$ is

$$P(\phi, \alpha, \beta, \gamma | \mathbf{w}_{1:J}) \propto P(\mathbf{w}_{1:J} | \phi, \alpha, \gamma) P(\phi | \beta) P(\alpha, \beta, \gamma), \quad (3)$$

where the likelihood term $P(\mathbf{w}_{1:J} | \phi, \alpha, \gamma)$ is given by Equation 2. This distribution is intractable (as is even the likelihood term itself), and as such it is necessary to use Markov Chain Monte Carlo (MCMC) methods to sample from it.

There are different options available for MCMC sampling. The method we employ is a Gibbs sampler that draws samples from the posterior over α , β , γ and $\mathbf{x}_{1:J}$. Here, $\mathbf{x}_{1:J}$ are the sequences of latent-variables for each of the J texts, i.e. $\mathbf{x}_1, \mathbf{x}_2 \dots \mathbf{x}_J$, with $\mathbf{x}_j = x_{j1} \dots x_{jn_j}$. This Gibbs sampler has the useful property of integrating over ϕ , $\pi_{1:J}$ and $\theta_{1:J}$, which entails both computational efficiency and faster convergence.

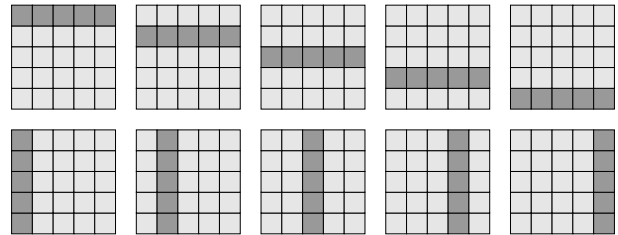
²The β parameters can be seen as a prior over ϕ , but a prior that will be inferred from the data rather than simply assumed.

On convergence of the Gibbs sampler, we will obtain samples from the joint posterior distribution $P(\mathbf{x}_{1:J}, \alpha, \beta, \gamma | \mathbf{w}_{1:J})$. From this, other variables of interest can be obtained. For example, it is desirable to know the likely values of the topic distributions $\phi_1 \dots \phi_k \dots \phi_K$. Given known values for $\mathbf{x}_{1:J}$ and β , the posterior distribution over ϕ is simply a product of Dirichlet distribution, from which samples are easily drawn and averaged. Further details of this Gibbs sampler are provided in the Appendix.

Demonstration

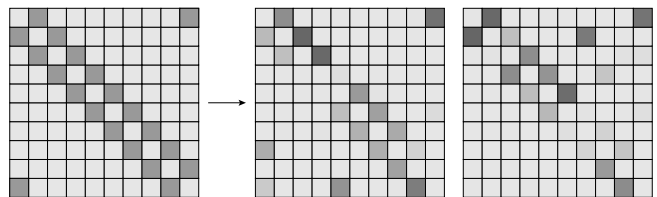
Here, we demonstrate the operation of the HMTM on a toy problem. In this problem, we generate a data-set from a HMTM with known values for ϕ , α and γ . We can then train another HMTM, whose parameters are unknown, with this training data-set. Using the Gibbs sampler, we can draw samples from the posterior over ϕ , α , β and γ , and then compare these samples to the true parameter values that generated the training data.

In the example we present here, we use a “vocabulary” of $V = 25$ symbols, and a set of $K = 10$ “topics”. As is common practice in demonstrations of related models, the “topics” we use in this example can be visualized using the grids shown below.



Each grid, although shown as a 5×5 square, is just a 25 dimensional array, with 5 high values (darker) and 20 low values (lighter). Each of these arrays corresponds to one of the topics distributions in our toy problem, i.e. each one places the majority of its probability mass on a different set of 5 symbols.

The $\gamma_1 \dots \gamma_K \doteq \gamma$ parameters in the HMTM are a set of K K -dimensional Dirichlet parameters. Each γ_k is an array of K non-negative real numbers. A common reparameterization of Dirichlet parameters, such as γ_k is as $s\mathbf{m}_k$, where s is the sum of γ_k and \mathbf{m}_k is the γ_k divided by s . For each set of K Dirichlet parameters, we used an $s = 3.0$. The K arrays $\mathbf{m}_1 \dots \mathbf{m}_K$ are depicted below on the left.



From these Dirichlet parameters, we may generate arbitrarily many sets of state-transition parameters for a 10

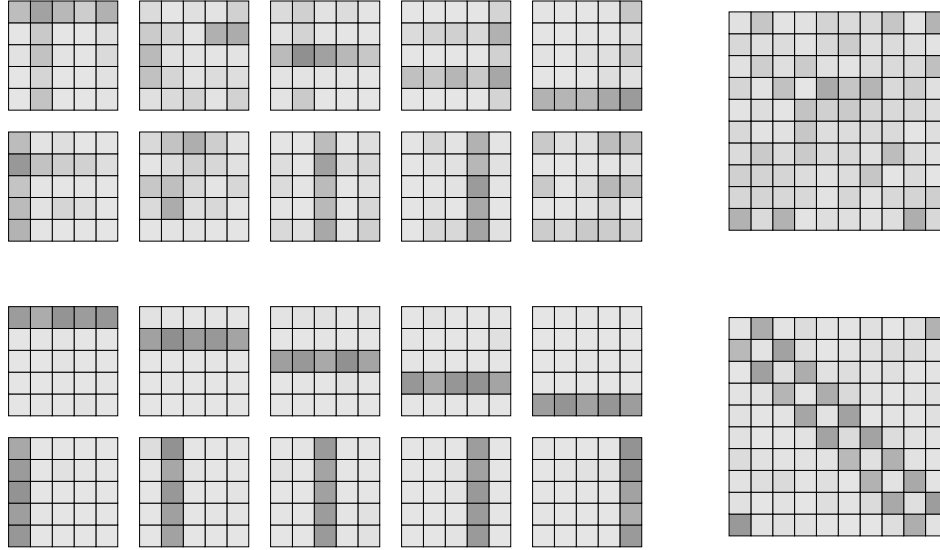


Figure 3: Averages of samples from the posterior distribution over the topic distributions (left) and locations of the γ parameters (right). Shown on the top row are averages, over 10 draws, drawn after 20 iterations. Shown on the lower row are averages, again over 10 draws, taken after 100 iterations. Compare with the true parameters shown on the previous page.

state HMM. As an example, we show two such sets on the right. As is evident, these parameters retain characteristics of the patterns found in the original Dirichlet parameters. We can see that, on average, the state transition dynamics leads a given state to map to either the state before it, or the state after it. For example, we can see that, on average, state 2 maps to state 1 or state 3, state 3 maps to state 2 or state 4, and so on. While this average dynamical behavior is simple, it is not trivial, and does not lead to fixed point or periodic trajectories. Note also that the small differences in the transition dynamics can lead to quite distinct dynamical behaviors in their respective HMMs.

On the basis of these ϕ and θ , and using an array of K ones as the parameters α , we generated $J = 50$ training “texts” as follows. For each text j , we drew a set of initial conditions and transition parameters for a HMM from α and γ , respectively. We then iterated the HMM for $n_j = 100$ steps, to obtain a state trajectory $x_{j1} \dots x_{jn_j}$. On the basis of the value of each x_{ji} , we chose the appropriate topic (i.e. if $x_{ji} = k$ we chose ϕ_k) and drew an observation w_{ji} from it. The training thus comprised a set of J symbol sequences, with each symbol taken a value from the set $\{1 \dots 25\}$.

Using this as training data, we trained another HMTM whose parameters were unknown. As described earlier, the Gibbs sampler draws samples from the posterior distribution over $\mathbf{x}_{1:J}$, α , β and γ . From these samples, we may also draw samples from the posterior over the topics. In Figure 3, we graphically present some results of these simulations. Show in this figure are averages of

samples drawn from the posterior over ϕ and $\mathbf{m}_1 \dots \mathbf{m}_k$, i.e the location parameters of $\gamma_1 \dots \gamma_k$. On the top row of Figure 3, we show averages of samples drawn after 20 iterations of the sampler. On the lower row, we show averages of drawn after 100 iterations. In both cases, these averages are over 10 samples taken two iterations apart in time. To the left in each case, are the inferred topics. To the right are the inferred locations of the Dirichlet parameters. These inferred parameters can be compared to the true parameters on the previous page. By doing so, it is clear that even after 20 iterations of the sampler, patterns in the topic distributions have been discovered. After 100 iterations, the inferred parameters are almost identical to the originals.

Although not shown, the Gibbs sampler also successfully draws samples from the posterior over α , β^3 and the scale parameter s for γ . In addition, we may use draws from the posterior to estimate, using the harmonic mean method, the marginal likelihood of the model under a range of different numbers of topic distributions. Although, the harmonic mean method is not highly recommended, we have found that in practice it consistently leads to an estimate of the correct number of topics.

Learning Topics from Text

In this final section, we present some topics learned by a HMTM trained on a corpus of natural language. The corpus used was a sub-sample from the British National

³For the case of β , we used a symmetric Dirichlet distribution.

HMTM Topics	beer	sheep	sugar	aircraft	film	say	ship
	guinness	cattle	fruit	plane	movie	know	boat
	alcohol	meat	butter	jet	series	talk	ferry
	ale	livestock	bread	airline	tv	think	vessel
	whisky	dairy	chocolate	squadron	story	feel	ships
	spirits	beef	milk	helicopter	television	understand	navy
	wine	pigs	cream	fighter	soap	believe	shipping
	cider	animal	water	hercules	movies	speak	lifeboat
pint	cow	lemon	airbus	drama	ask	fleet	
lager	pig	egg	falcon	episode	explain	coastguard	
Standard Topics	pub	farm	fruit	air	film	want	boat
	drink	agriculture	add	aircraft	star	think	island
	guinness	food	fresh	flight	hollywood	like	sea
	beer	farming	butter	plane	movie	people	ship
	drinking	sheep	cooking	airport	screen	moment	crew
	wine	agricultural	minutes	flying	stars	happen	ferry
	bar	cattle	hot	pilot	director	wanted	sailing
	alcohol	ministry	food	fly	actress	worried	yacht
brewery	crop	bread	jet	actor	believe	shipping	
whisky	pigs	chicken	airline	role	exactly	board	

Table 1: Examples of topics learned by a HMTM (top row) that was trained on a set of documents taken from the BNC. On the lower row, we show topics from a standard topics model also trained on a set of documents from the BNC.

Corpus (BNC)⁴. The BNC is annotated with the structural properties of a text such as sectioning and subsectioning information. The latter type of annotation facilitates the processing of the corpus. To extract texts from the BNC we extracted contiguous blocks that were labeled as high-level sections, roughly corresponding to individual articles, letters or chapters. These sections varied in size from tens to thousands of words, and from these we chose only those texts that were approximately 150-250 words in length. This length is typical of, for example, a short newspaper article. Following these criteria, we then sampled 2500 individual texts to be used for training. Of all the word types that occurred within this subset of texts, we excluded words that occurred less 5 times overall, and replaced their occurrence with a marker symbol. This restriction resulted in a total of 5182 unique words.

We trained a HMTM with $K = 120$ topics using this corpus. After a burn-in period of 1000 iterations, we drew 50 samples from the posterior over the latent trajectories and β , with each sample being 10 iterations apart. We used these to draw samples from the pos-

terior over the topics, which are then averaged, as described earlier. In the upper part of Table 1, we present seven averaged topics from the HMTM simulation. For the purposes of comparison, in the lower part Table 1 we present seven averaged topics taken from a standard topics model. This standard topics model was trained on a larger corpus, and is described in detail in Andrews et al. (In Press). The topics in the standard model were chosen by finding the topics that are the closest matching to the HMTM topics we chose.

The side-by-side comparison provides an appreciation for how the topics in a HMTM differ from the standard model. In the HMTM, the topics are more refined in the semantics, referring to more specific categories of things or events. For example, we see that the first topic to the left in the HMTM refers to alcoholic beverages, specifically those associated with a (British) pub. By contrast, the corresponding topic from the standard model is less specifically about beverages and refers more generally to things of, or relating to, pubs. In the next example, we see that the topic from the HMTM refers to farm animals. By contrast, the corresponding topic from the standard model is less specifically about farm animals and more related to agriculture in general. In all of the examples shown, a similar pattern of results holds.

Conclusion

The aim of this paper is to demonstrate how to extend the standard Topics model so as to learn more fine-

⁴The BNC is a 100 million word corpus of contemporary written and spoken English in the British Isles. According to its publishers, the texts that make up the written component include “extracts from regional and national newspapers, specialist periodicals and journals for all ages and interests, academic books and popular fiction, published and unpublished letters and memoranda, school and university essays”.

grained semantic representations from the statistics of language. This is done by using the sequential statistical information of language. As mentioned, the sequential order in which words occur provide vital information about the possible meaning of words. This information is not available in the standard Topics model, nor in most of its counterparts. In the examples shown, we have seen that more refined semantic representations can be learned when sequential information is taken into account.

This general usefulness of sequential information can be understood by way of a, albeit contrived, simple example. Words like *horse*, *cow*, *mule* are likely to occur as subjects of verbs like *eat*, *chew*, while words like *grass*, *hay*, *grain* are likely to occur as their objects. A model that learns topics by taking into account this sequential information may learn that words like *horse*, *cow*, and *mule* etc., form a coherent topic. Likewise, such a model may infer other topics based on words like *eat*, *chew*, etc., or words like *grass*, *hay*, *grain*, etc. By contrast, the standard Topics model, based on the assumptions that the sequential information in a text is irrelevant, is likely to conflate these separate topics into one single topic referring to, for example, *farms* or *farming*.

Appendix

The Gibbs sampler for the HMTM model draws samples from $P(\mathbf{x}_{1:J}, \boldsymbol{\alpha}, \boldsymbol{\beta}, \boldsymbol{\gamma} | \mathbf{w}_{1:J})$. It does so iteratively sampling from a given latent variable x_{ji} , assuming values from all other latent variables, and for $\boldsymbol{\alpha}$, $\boldsymbol{\beta}$, $\boldsymbol{\gamma}$. The conditional distribution over x_{ji} is given by

$$P(x_{ji} | \mathbf{x}_{-[ji]}, \mathbf{w}_{1:J}, \boldsymbol{\alpha}, \boldsymbol{\beta}, \boldsymbol{\gamma}) \propto P(w_{ji} | x_{ji}, \mathbf{x}_{-[ji]}, \mathbf{w}_{-[ji]}, \boldsymbol{\beta}) P(x_{ji} | \mathbf{x}_{-[ji]}, \boldsymbol{\alpha}, \boldsymbol{\gamma}), \quad (\text{A.1})$$

where we denote the set of latent variables excluding x_{ji} by $\mathbf{x}_{-[ji]}$, and denote the set of observables excluding w_{ji} by $\mathbf{w}_{-[ji]}$. Superficially, this conditional distribution appears identical to the conditional distributions in the Gibbs sampler for the standard Topics model, as described in Griffiths and Steyvers (2002, 2003); Griffiths et al. (2007). However, due to the non-independence in the latent trajectory that results from the Markov dynamics, the term $P(x_{ji} | \mathbf{x}_{-[ji]}, \boldsymbol{\alpha}, \boldsymbol{\gamma})$ must be calculated as a ratio of Polya distributions, i.e.

$$P(x_{ji} | \mathbf{x}_{-[ji]}, \boldsymbol{\alpha}, \boldsymbol{\gamma}) = \frac{P(\mathbf{x}_{1:J} | \boldsymbol{\alpha}, \boldsymbol{\gamma})}{P(\mathbf{x}_{-[ji]} | \boldsymbol{\alpha}, \boldsymbol{\gamma})}. \quad (\text{A.2})$$

The Dirichlet parameters $\boldsymbol{\alpha}$, $\boldsymbol{\beta}$, $\boldsymbol{\gamma}$ may also be sampled by Gibbs sampling. For example, each γ_k is reparameterized as $s\mathbf{m}_k$ (as described in the main text). Assuming known values for all variables, the conditional posterior distribution of s is log-concave and can be sampled using Adaptive Rejection sampling (ARS), see Gilks and Wild (1992). Likewise, assuming known values for all other

variables, the conditional posterior over the share of the probability mass between any two elements of \mathbf{m}_k is also log-concave and can be sampled by ARS. As such, the Gibbs sequentially samples from each latent variable x_{ji} , each scale parameter of the Dirichlet parameters given by $\boldsymbol{\alpha}$, $\boldsymbol{\beta}$, $\boldsymbol{\gamma}$, and also from the share of probability mass between every pair of elements of each location parameters of the Dirichlet parameters.

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